

Analysis of the Equations of the Form $m = \frac{i}{(1-n)^{\frac{1}{2}}}$

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Abstract: In this work, the equation of the form $m = \frac{i}{(1-n)^{\frac{1}{2}}}$

was analysed

Key words: Real ,positive, negative and imaginary numbers and quadratic
equations

MSC: 08C99

Let $m = \frac{i}{(1-n)^{\frac{1}{2}}}$ where i is imaginary, m and n are real (1)

Squaring $m^2(1-n) = i^2$ (2)

Replacing i by -1 , $m^2(n-1) = 1$ (3)

$$\text{i.e.,} \quad m^2 n = m^2 + 1 \quad (4)$$

$$\therefore n = 1 + \frac{1}{m^2} \quad (4a)$$

Multiplying (3) by (n+1), $m^2(n^2 - 1) = n + 1$

$$\text{i.e.,} \quad m^2 n^2 - m^2 - n - 1 = 0 \quad (5)$$

Equation (5) is quadratic in n

$$\begin{aligned} \therefore n &= \frac{1 \pm [1 + 4m^4 + 4m^2]^{\frac{1}{2}}}{2m^2} \\ &= \frac{1 \pm [(2m^2 + 1)^2]^{\frac{1}{2}}}{2m^2} \\ n &= \frac{1 \pm 2m^2 + 1}{2m^2} \end{aligned} \quad (6)$$

$$\text{Taking positive value, } n = \frac{2 + 2m^2}{2m^2}, \text{ i.e., } n = 1 + \frac{1}{m^2} \quad (6a)$$

$$\text{Taking negative value in (6), } n = -1. \quad (7)$$

According to the laws of quadratic equations the roots, $\alpha + \beta = -B/A$ and $\alpha\beta = C/A$.

$$\text{So,} \quad \alpha + \beta + \alpha\beta = \frac{C - B}{A}. \text{Applying this relation in (5)}$$

$$\alpha + \beta + \alpha\beta = \frac{C - B}{A} = -1$$

$$\text{i.e.,} \quad \alpha + \beta + \alpha\beta + 1 = 0$$

$$\text{i.e.,} \quad \alpha(1 + \beta) + (1 + \beta) = 0$$

$$\text{i.e.,} \quad (1 + \alpha)(1 + \beta) = 0 \quad (7a)$$

$$\text{i.e.,} \quad \alpha = -1 \quad (7b)$$

(7) and (7b) are one and the same result.

From (7a) we get, $(1 + \beta) = 0$

$$\text{Putting (6a) in the above relation, } 1 + \frac{1}{m^2} + 1 = 0$$

$$\text{i.e.,} \quad 2m^2 + 1 = 0$$

$$\text{i.e., } m^2 = \frac{-1}{2}$$

Taking square root on both sides, $m = \frac{i}{\sqrt{2}}$ (8)

Applying (8) in (1), $\frac{i}{\sqrt{2}} = \frac{i}{(1-n)^{\frac{1}{2}}}$

Squaring on both sides, $\frac{i^2}{2} = \frac{i^2}{1-n}$
i.e., $n = -1$ (9)

(7) and (9) are one and the same.

The above analysis establishes that α and β are distinct. (10)

According to the laws of quadratic equations of the general form $Ax^2 + Bx + C = 0$, the roots are distinct iff $B^2 - 4AC \neq 0$ (11)

Assuming (11) in (5), $1 + 4m^2 + 4m^4 = 0$

i.e., $(1 + 2m^2)^2 = 0$

I.e., $1 + 2m^2 = 0$

i.e. $m^2 = \frac{-1}{2}$

Taking square root on both sides, $m = \frac{i}{\sqrt{2}}$ (12)

Equations (8) and (12) are one and the same.

Putting (12) in (1) we have $n = -1$ (13)

Putting $n = -1$ in (5) the equation satisfies.

The above analysis shows as clear as crystal that $n = -1$

. is the only consistent solution for (5) (14)

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