



point B of the wave which will arrive on SS' at B<sub>1</sub>, at time  $t$  such that

$$BB' = ct, \quad B_1B' = vt = \beta ct.$$

From B<sub>1</sub> we lead tangent B<sub>1</sub>A<sub>1</sub> to the circle of ray  $ct$  with center at A, being at angle  $x$  with SS'. B<sub>1</sub>A<sub>1</sub> will be the trace of the wave in the driven part of the ether (who is at rest relative with the chosen axes).

In triangle BB'B<sub>1</sub>, we have

$$\frac{BB_1}{\cos(\alpha + i)} = \frac{\beta ct}{\sin(i' - i)} = \frac{ct}{\cos(\alpha + i')}.$$

In addition, in triangle ABB<sub>1</sub>,

$$\frac{AB_1}{\cos(i' - i)} = \frac{BB_1}{\sin i}$$

and finally

$$AA_1 = ct = AB_1 \sin r.$$

From where one draws

$$\sin r = \frac{\cos(\alpha + i')}{\cos(\alpha + i)} \frac{\sin i}{\cos(i' - i)} = \frac{\sin i' - \beta \cos i' \cos(\alpha + i')}{1 + \beta \sin(\alpha + i')} = \sin i' - \beta \cos \alpha,$$

by limiting us to the first order of approximation.

The deviation  $\Delta'$  of the luminous ray will equal  $i' - r$ , from where

$$2 \sin \frac{\Delta'}{2} \cos \left( i' + \frac{\Delta'}{2} \right) = \beta \cos \alpha,$$

One would obtain the same result by making calculation by means of motionless axes in which ether not entrained.

III. In the ordinary theory, where the ether is supposed absolutely motionless, the deviation has as a value

$$\Delta = \beta \cos(\alpha + i),$$

then  $\Delta'$  can be expressed as

$$\Delta' = \beta \left[ \cos(\alpha + i) + \tan i \sin(\alpha + i) \right].$$

The difference between the two values is equal to

$$\Delta' - \Delta + \beta \tan i \sin(\alpha + i).$$

Taking into account that the observer can only see stars located above the horizon and we denote by  $h$  and  $R$  the thickness of the entrained ether bubble and the radius of the earth, one sees easily that

$$\sin i \leq \frac{R}{R+h},$$

where the real limit is still lower than this value because the observation of low stars on the horizon is difficult.

It seems natural to assume that the thickness of the ether bubble is large compared to the Earth's radius; if  $h$  is on the order of at least  $100R$ , the value of  $\Delta' - \Delta$  will remain below  $10^{-2} \beta$  and will be inappreciable.

IV. One may feel reluctant with the idea that the ether bubble is entrained as a block, and so we assume that the ether is involved gradually, with speeds decreasing up to zero as one moves away sufficiently, and, in this case especially, it seems natural to consider that the layer where the speed of ether vanishes is extremely far away from the Earth.

Between two infinitely close layers, one will still have

$$d\Delta' = \frac{\cos \alpha}{c \cos i} dv$$

However  $i$  has only first order variations, therefore  $\cos i$  can be regarded as constant for integration and one finds, while limiting oneself to the first order of approximation, the preceding formula

$$\Delta' = \beta \frac{\cos \alpha}{\cos i}.$$

V. It follows from this that the aberration of stars, so much at least that we have not significantly increased the precision of observations for stars relatively low on the horizon, does not settle the question of the entraining or the not-entraining of ether by the Earth, and it seems likely in the event of entraining, this entraining extends to long distances from the Earth.

*[translator's note: Reader is advised to see:*

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*available at: <http://www.wbabin.net/pprhst.htm#Metz> ]*