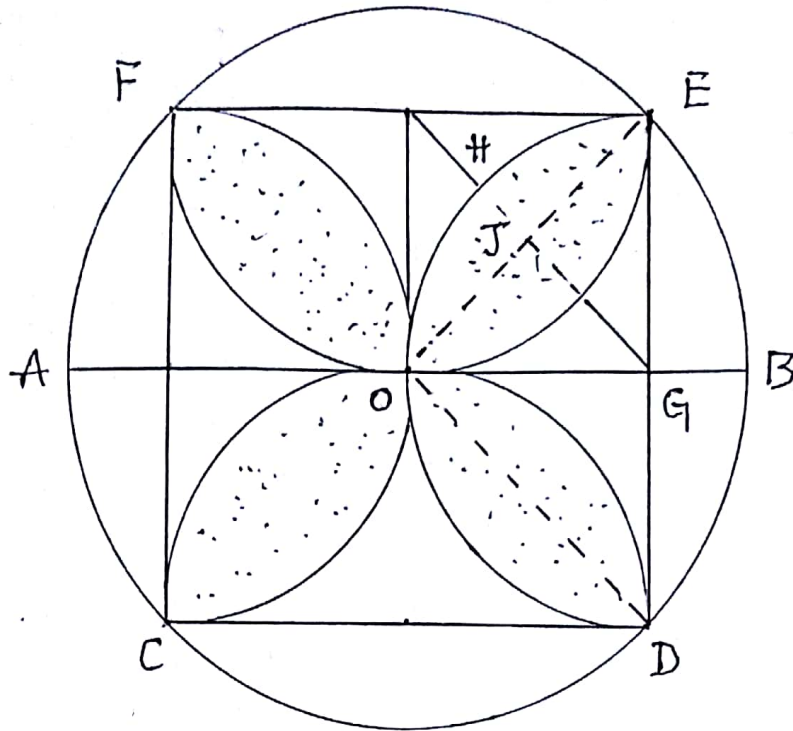


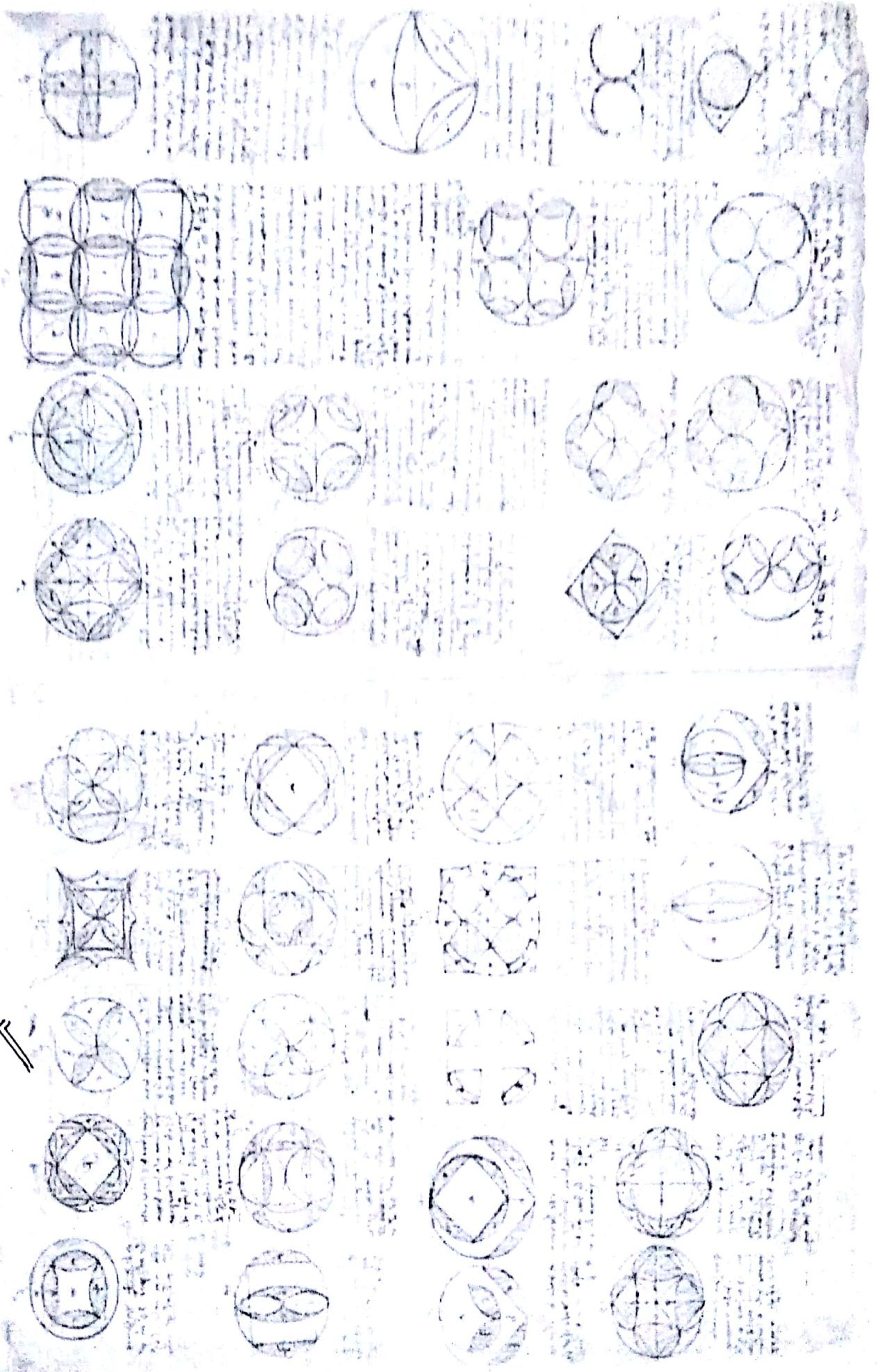
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# LEONARDO DA VINCI SQUARED A CIRCLE



1. Circle
2. Diameter =  $AB = a$
3. Radius =  $OB = \frac{a}{2}$
4. Triangle =  $EOD$
5. Base =  $DE = \frac{\sqrt{2}a}{2}$
6. Altitude =  $GD = \frac{\sqrt{2}a}{4}$
7. Area of Triangle =  $\frac{1}{2}ab = \frac{1}{2} \times \frac{\sqrt{2}a}{4} \times \frac{\sqrt{2}a}{2}$   
 $= \frac{a^2}{8}$

Fig. 9. Leonardo da Vinci, *Codex Atlanticus*, folio 471. Squaring the circle, graphic research



8. Sector = EODB =  $\frac{1}{4}$ th Circle = Quadrant

9. Area of Circle =  $\frac{\pi a^2}{4}$

10. Area of Quadrant =  $\frac{\pi a^2}{16}$

11. Segment = EODB

12. Area of Segment = Quadrant - Triangle

$$= \frac{\pi a^2}{16} - \frac{a^2}{8} = \left(\frac{\pi-2}{16}\right)a^2$$

13. Area of 4 Segments =  $4\left(\frac{\pi-2}{16}\right)a^2 = \left(\frac{\pi-2}{4}\right)a^2$

14. In the Circle there are 4 Petals.  
Petals are shaded with dots.

15. We have smaller quadrant OGEH.

16. And also smaller triangle = EOG

17. Base = OE =  $\frac{a}{2}$

18. Altitude = JG =  $\frac{a}{4}$   
small

19. Area of Triangle =  $\frac{1}{2}ab = \frac{1}{2} \times \frac{a}{4} \times \frac{a}{2}$   
=  $\frac{a^2}{8}$

20. Area of smaller quadrant: 16

21. Radius = GH =  $\frac{\sqrt{2}a}{2}$  = Diameter =  $\frac{\sqrt{2}a}{2}$

22. Area of Circle =  $\frac{\pi a^2}{4} = \frac{\pi}{4} \times \frac{\sqrt{2}a}{2} \times \frac{\sqrt{2}a}{2}$   
= where diameter =  $\frac{\sqrt{2}a}{2}$

Ex 3 # 4

23. Area of Circle =  $\frac{\pi}{4} \times \frac{\sqrt{2}a}{2} \times \frac{\sqrt{2}a}{2}$   
 $= \frac{\pi}{4} \times \frac{2a^2}{4} = \frac{\pi a^2}{8}$

24. Area of Quadrant =  $\frac{1}{4}$ th of Circle  
 $= \frac{\pi a^2}{8} \times \frac{1}{4} = \left(\frac{\pi}{32}\right) a^2$

25. Area of the small segment = HOJE  
 Small Quadrant - Small triangle

26.  $= \frac{\pi a^2}{32} - \frac{a^2}{16} = \left(\frac{\pi-2}{32}\right) a^2$

27. In each petal there are two small segments

28. Area of each Petal =  $\left(\frac{\pi-2}{32}\right) a^2 \times 2$

$= \left(\frac{\pi-2}{16}\right) a^2$

29. There are 4 petals =  $\left(\frac{\pi-2}{16}\right) a^2 \times 4$

$= \left(\frac{\pi-2}{4}\right) a^2$

30. Area of 4 Segments =  $\left(\frac{\pi-2}{4}\right) a^2$   
 Refer S.No. 13

So, Area of 4 Petals = Area of 4 Segments  
 (S.No. 29) (S.No. 30)  
 S.No. 13

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The areas of the 4 segments is equal to the areas of the 4 petals.

"It follows that the unshaded area within the circle is equal to that of the square CDEF."

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Conclusion:

1. C. L. F. Lindemann (1882) has said  $\pi$  is a transcendental number.
2. It implies that Squaring of circle is impossible.
3. In this paper we see that Leonardo da Vinci has squared a circle.
4. Who is Right and Who is Wrong?
5. Hippocrates of Chios (450 BC) has squared a circle, semicircle and lunes.
6. Leonardo da Vinci also has squared a circle.

7. On what basis C.L.F. has said  $\pi$  is a transcendental number?

The answer is: it is based on Euler's formula  $= e^{i\pi} + 1 = 0$

8. Let us analyse it:

In the <sup>above</sup> formula  $\pi$  refers to  $\pi$  radians  $180^\circ$ .

If  $\pi$  constant 3.14 is involved the Euler's formula becomes wrong. In other words, the Euler's formula  $e^{i\pi} + 1 = 0$  rejects the  $\pi$  constant.

9. The question is:

How can we or Lindemann say the rejected  $\pi$  constant as a transcendental number based on Euler's formula.

10. Prof. Underwood Dudley has questioned Lindemann's proof based on the approximate values of  $e$ ,  $i$  and  $\pi$ .

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